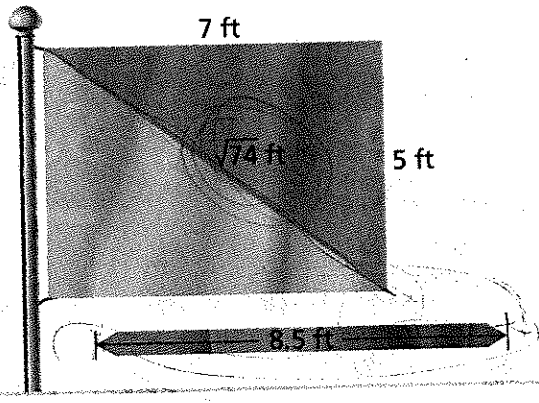


EXAMPLE 1 Approximate an Irrational Number

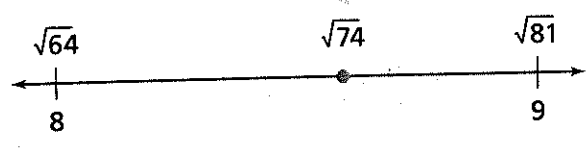


Darcy wants to add the ribbon shown along the diagonal of the rectangular flag she is designing. Does Darcy have enough ribbon? Explain.



Approximate $\sqrt{74}$ using perfect squares.
 Because 74 lies between the two consecutive perfect squares 64 and 81, $\sqrt{74}$ is located between $\sqrt{64}$ and $\sqrt{81}$.

Because 74 is closer to 81 than 64, $\sqrt{74}$ is closer to $\sqrt{81}$, or 9.

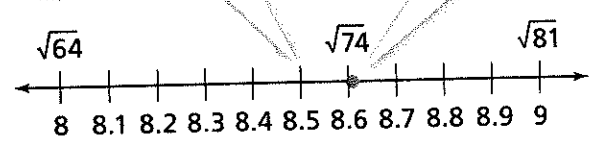


Find a better approximation by squaring decimals between 8 and 9. Then compare.

Reasoning Which decimals can you use to find a better approximation? **MP.2**

$8.5 \times 8.5 = 72.25$
 This approximation is too low.

$8.6 \times 8.6 = 73.96$
 This is a good approximation.



The length of the diagonal, $\sqrt{74}$, is about 8.6 feet.
 Darcy does not have enough ribbon. *8.6 feet*

Try It!

Between which two whole numbers is $\sqrt{12}$?

$11 < 12 < 13$
 $\sqrt{9} < \sqrt{12} < \sqrt{16}$
 $3 < \sqrt{12} < 4$

Convince Me! Which of the two numbers is a better estimate for $\sqrt{12}$? Explain.

$$\begin{array}{r} 3.5 \\ \times 3.5 \\ \hline 175 \\ 1050 \\ \hline 1225 \end{array}$$

12.25

$$\begin{array}{r} 3.4 \\ \times 3.4 \\ \hline 136 \\ 1024 \\ \hline 1156 \end{array}$$

$\sqrt{12} \approx 3.5$

$$\sqrt[3]{288}$$

$$\sqrt{25} \quad \sqrt{36}$$

$$5 \quad 6$$

$$\begin{array}{r} 5.3 \\ \times 5.3 \\ \hline 159 \\ 2650 \\ \hline 28.09 \end{array}$$

1.09

$$\begin{array}{r} 5.2 \\ \times 5.2 \\ \hline 104 \\ 2600 \\ \hline 27.04 \end{array}$$

1.96

$$\sqrt{28} \approx 5.3$$

$$\sqrt[5]{792}$$

$$\sqrt{64} \quad \sqrt{81}$$

$$8 \quad 9$$

$$\begin{array}{r} 8.8 \\ \times 8.8 \\ \hline 704 \\ 7040 \\ \hline 77.44 \end{array}$$

1.56

$$\begin{array}{r} 8.9 \\ \times 8.9 \\ \hline 801 \\ 7120 \\ \hline 79.21 \end{array}$$

21

$$\sqrt{79} \approx 8.9$$

Order from least to greatest

$$\pi^2, 9\frac{1}{2}, 9.8, 9.\overline{5}, \sqrt[9]{94}, \sqrt{94}$$

$$\begin{array}{r} 3.14 \\ 3.14 \\ \hline 1256 \\ 3140 \\ 94200 \\ \hline 98596 \end{array}$$

$$\begin{array}{r} 9.7 \\ 9.7 \\ \hline 1679 \\ 8730 \\ \hline 94.09 \end{array}$$

$$9\frac{1}{2}, 9.\overline{5}, \sqrt{94}, 9.8, \pi^2$$

$$\begin{array}{r} 9.6 \\ \times 9.6 \\ \hline 576 \\ 8640 \\ \hline 92.16 \end{array}$$

$$\sqrt{94} \approx 9.7$$